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1	UNITED STATES PATENT AND TRADEMARK OFFICE
2	BEFORE THE PATENT TRIAL AND APPEAL BOARD
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4	GOOGLE, INC., and YOUTUBE, LLC,)
5) Detitionen
6	Petitioner,)
7	vs.)) Case No. IPR2015-00347
8	NETWORK-1 TECHNOLOGIES, INC.,)
9	Patent Owner.)
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16	VIDEOTAPED DEPOSITION OF PIERRE MOULIN, PhD
17	VOLUME I
18	Santa Monica, California
19	Wednesday, August 19, 2015
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21	
22	NETWORK-1 EXHIBIT A2006
23	Google Inc. v. Network-1 Technologies, Inc.
24	REPORTED BY: RICH ALOSSI, RPR, CCRR, CSR NO. 13497
25	Job No: 96808

	Page 2
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16	VIDEOTAPED DEPOSITION OF PIERRE MOULIN, PhD,
17	VOLUME I, taken on behalf of the Patent Owner, at 201
18	Santa Monica Boulevard, Sixth Floor, Santa Monica,
19	California, on Wednesday, August 19, 2015, from 9:02 AM to
20	5:39 PM, before RICH ALOSSI, RPR, CCRR, CSR NO. 13497.
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1	SANTA MONICA, CALIFORNIA; WEDNESDAY, AUGUST 19, 2015	
2	9:02 AM - 5:39 PM	
3		
4	THE VIDEOGRAPHER: Good morning. This is the	
5	start of Tape Number 1 of the videotaped deposition	
6	of Pierre Moulin in the matter of Google,	
7	Incorporated, and YouTube, LLC, versus Network-1	
8	Technologies, Incorporated. This case is before the	
9	US Patent and Trademark Office, Patent Trial and	
10	Appeal Board. Case number is IPR2015-00347.	
11	This deposition is being held at 201 Santa	
12	Monica Boulevard, on the sixth floor, in	
13	Santa Monica, California. Today's date is	
14	August 19th, 2015. The time is 9:03 AM.	
15	My name is Scott McNair from TSG	
16	Reporting, Incorporated. I'm the legal video	
17	specialist. The court reporter today is	
18	Rich Alossi, also in association with TSG Reporting.	
19	Will counsel please identify yourselves	
20	for the record.	
21	MR. DOVEL: My name is Greg Dovel. I	
22	represent the patent owner, Network-1.	
23	MR. ELACQUA: My name is Jim Elacqua with	
24	Skadden Arps, here to represent Google and YouTube.	
25	MR. CHEN: Ian Chen with Skadden, also on	

behalf of Google and YouTube. 1 2 MR. SONNENTAG: Rich Sonnentag, in-house 3 counsel at Google. MR. FENSTER: Marc Fenster with Russ, August & 4 5 Kabat, representing the patent holder in the 6 litigation. 7 THE VIDEOGRAPHER: Thank you. Will the court 8 reporter please swear in the witness. THE REPORTER: Please raise your right hand. 9 10 Do you solemnly state that the testimony 11 you are about to give in the matter now pending 12 shall be the truth, the whole truth and nothing but the truth? 13 14 THE WITNESS: I do. 15 THE REPORTER: Thank you. We're on the record. 16 17 18 PIERRE MOULIN, PhD, 19 having been first duly sworn by 20 the court reporter, was examined 21 and testified as follows: 22 23 EXAMINATION 24 BY MR. DOVEL: 25 Your name is pronounced -- is it Moulin? Q

1	A Yes. Almost.
2	Q Dr. Moulin?
3	A Yes.
4	Q Now, Dr. Moulin, you're familiar with the
5	concept of whether or not an algorithm is sublinear?
6	A Yes.
7	Q Were you familiar with that before you
8	started work on this case?
9	A Yes.
10	Q Is the concept of whether an algorithm is
11	sublinear with respect to the database size that
12	it's used over, is that a concept that's common in
13	your field?
14	A Yes.
15	Q When is it during the course of one's
16	education that one would learn about the concept of
17	sublinear?
18	A The concept of sublinear arises in man $rac{1}{2}$
19	contexts, not just databases. The first time
20	someone would be exposed to that would be typically
21	in a university course, depending on their field.
22	Q When you say "university course," what
23	course would that be?
24	MR. ELACQUA: It depends on the field. So it
25	could be in computer science. Often that might be

Page 9 introduced at the senior level, or if it's 1 2 electrical engineering, that might also be 3 introduced around the same time. Each program is a different curriculum. 4 5 MR. DOVEL: I'm going to mark as Exhibit 6 Number 1004-237 the Declaration of Dr. Moulin from the case related to the '237 patent. 7 8 (Exhibit 1004-237 was marked for 9 identification by the court reporter and is 10 attached hereto.) 11 MR. DOVEL: I've placed that in front of the 12 witness. 13 BY MR. DOVEL: In your Declaration that I've placed in 14 Ο 15 front of you, you provide a definition of the concept of sublinear execution time; is that 16 correct? 17 18 Α Where? 19 Pages 19 to 20 of your Declaration. Q 20 That is correct, yes. Α 21 Q Now, on page 20 you've got a diagram that 22 illustrates the concept of what is a sublinear search and what is a linear search; correct? 23 24 Α It illustrates it, yes. 25 Is it the case that if we have a linear 0

search, that it will have a constant slope as you've 1 2 depicted in your diagram there? "Constant slope" in terms of -- in terms 3 Α of the number of entries in the search database, you 4 5 Is that what you mean? mean? 6 Yes. Yes. 0 7 Α In this example, yes. 8 Ο Is it the case that as sublinear is used 9 in the patent, it's going to result in a scaling of the search time compared to the size of the database 10 such that it will have a constant slope? 11 12 You say if it is a linear search? Α 13 If it's a linear search. Right. 0 So let me give you a different question. 14 15 Α Only in this example, yes. 16 Let me give you a different question so we 0 have a clean record. 17 18 If we have an algorithm that is a linear 19 search, is it the case that it will have a constant 20 slope if we plot the search time compared to the size of the database? 21 22 Α Yes. Is it the case that if we have a sublinear 23 \bigcirc 24 search, then the slope will curve down and approach 25 zero if we plot search time compared to the size of

Page 11

1 the database?

- 2
- A Not necessarily.

3 Q When wouldn't it do that?

A Because this is an example that shows only how search time is as a function of number of entries in the search database. But that's not the only criterion.

8 Q What's the other criteria?

9 A Well, it's the size of the database that 10 matters. So number of entries is only one factor 11 that affects the size of the database.

12 Q Let's -- let's talk about the size of the 13 database, then.

14 Is it the case that if we have a sublinear 15 search as it's used in the Cox -- withdrawn.

16 When we're talking about the Cox patents, 17 do you understand we're talking about the four 18 patents that you filed declarations for in 19 connection with these proceedings before the PTAB?

20 A Yes.

Q If we have a sublinear search as it's used in the Cox patents, is it the case that if we plot search time compared to the size of the database over which we are searching, then the -- it will produce a curve such that it curves downward and 1 approaches zero?

2 Α You need to be more specific. Sublinear is mentioned in many places in all four patents in 3 slightly different contexts. So I would like you to 4 5 be more specific. Are you -- is it your testimony --6 0 withdrawn. 7 8 We're talking about sublinear as it's used in the claims of the patents. 9 10 Right. Α 11 You understand that some of the claims 0 12 have the phrase "sublinear search," some of them 13 have the phrase "sublinear time search"? That's my recollection. 14 Α Is it the case that sublinear search and 15 Ο sublinear time search mean the same thing in the 16 17 patents? 18 Α I would have to check every instance of 19 sublinear data. Used in different contexts, sometimes not defined precisely, you would have to 20 refer me to a specific instance. 21 22 Ο As the phrase "sublinear search" is used 23 in the claims of the patents, is it used 24 consistently, or does it mean different things in 25 the claims?

Page 13 It's used somewhat vaguely. 1 Α 2 I didn't ask whether it was vague. I want 0 to know does it mean the same thing or does it mean 3 different things? 4 5 I don't know. Because it's done vaguely, Ά 6 I cannot know for sure. You don't know one way or the other --7 Q 8 withdrawn. When you did your analysis and decided 9 that the prior art anticipates --10 11 Α Right. 12 -- and you decided that it disclosed a Ο 13 sublinear time search, what definition did you use? It's in relation to the size of the 14 Α database, which itself depends both on the number of 15 entries in the database and on the size of each 16 entry, each record. That's the standard definition. 17 18 That's the standard definition; right? Ο 19 Α Yes. 20 When you say "standard," you're talking Ο about the standard, well-known definition in the 21 22 art? 23 Α Yes. 24 And what it refers to, to be more precise, 0 25 is that if we have a sublinear search, that means

1	that the search time is going to grow at less than a
2	linear relationship compared to the size of the
3	database as we increase the size of the database?
4	A That is correct.
5	Q And we can increase the size of the
6	database either by increasing the number of entries
7	or by increasing the size of each entry in the
8	database?
9	A That is correct.
10	Q Is it the case that if we have a sublinear
11	search withdrawn.
12	Is it your understanding that the term
13	"sublinear search" and "sublinear time search" is
14	used in the patent claims to have that definition
15	that you just gave, the standard definition?
16	A Again, it has often not been defined
17	precisely. The word "sublinear" is used in a
18	slightly different context in the different patents.
19	When they say "sublinear," my
20	understanding is, again, consistent with the art. I
21	understand that to mean what we just discussed. So
22	it would mean what you just discussed.
23	So every time I read "sublinear" in the
24	patents, that's my understanding of it. Even though
25	it was not clearly defined.

Page 15 MR. DOVEL: I'm going to place in front of the 1 2 witness another exhibit which I'm going to mark as Exhibit 1001-237. This is the '237 patent. 3 (Exhibit 1001-237 was marked for 4 5 identification by the court reporter and is 6 attached hereto.) 7 BY MR. DOVEL: 8 Q I'd like you to turn to the claims of the 9 '237 patent. Do you see Claim 1 uses the phrase 10 "sublinear time search"? 11 Yes. 12 Α 13 Do you see Claim 5 uses the term Ο "sublinear time search"? 14 15 Α Yes. Does the phrase "sublinear time search," 16 Ο as it's used in the '237 patent claims, refer to a 17 search where the search time decreases at less than 18 a linear -- or increases at less than a linear rate 19 20 as we increase the size of the dataset over which 21 we're searching? 22 Α The claims do not say "as you increase the 23 size of the database." 24 If I read Claim 5, it reads, "A sublinear time search of extracted features of identified 25



a blank piece of notebook paper. And we're going to 1 make some notations on it. 2 (Exhibit 2005 was marked for identification 3 4 by the court reporter and is attached 5 hereto.) 6 MR. DOVEL: And the first thing I'm going to write is "O(n)." I'm going to stick that in front of 7 8 the witness. THE WITNESS: Okay. 9 BY MR. DOVEL: 10 11 Are you familiar with that notation? Ο 12 Yes. Α 13 What does that indicate to you, as one of 0 ordinary skill in the art? 14 15 Α So there's a parameter, N, which is a And one, let's say, looks at computational 16 number. time as a function of N. So if N grows, order N 17 means that the search time will not increase faster 18 than linearly. So it could increase linearly, or it 19 20 could increase sublinearly. 21 Ο What that tells us is that the upper bound for the increase in the execution time is going to 22 23 be linear; right? 24 At most linear. Α 25 Is it the case that -- withdrawn. 0

		Page
1	And there, when we see that withdrawn.	
2	In your field, when somebody writes that	
3	notation, O(n), they're using N to refer to the size	
4	of the dataset over which is being searched; is that	
5	right?	
6	A This is a very general notation in	
7	mathematics and computer science. So you can apply	
8	it to a database, for instance, where N could be the	
9	size of the database. That would be one	
10	application, yes.	
11	Q If N refers to the size of the dataset	
12	over which we're searching, then if we've got a	
13	database and what we know about it withdrawn.	
14	If N refers to the size of the database	
15	over which we're searching, and if we have an	
16	algorithm or search that performs at $O(n)$, as	
17	we've written there in Exhibit 2005, does what	
18	does that tell us about whether it's linear or	
19	sublinear?	
20	A It says it is at most linear. That's	
21	often a source of confusion, by the way. It means	
22	at most linear. It does not mean necessarily	
23	linear.	
24	Q That would indicate withdrawn.	
25	Is it the case that when scientists in	

18

your field are assessing the complexity of an 1 2 algorithm and how its execution time scales, that 3 it's based upon using a hypothetical dataset? 4 Α If you apply that notation to -- to a 5 dataset and you say N is the size of the dataset, 6 that would mean that the function on the left side, 7 which is a search time in your example, grows at 8 most linearly with N. 9 Ο If we have a -- let's assume we've got a -- another algorithm and what we know about it is 10 that its search time, compared to the size of the 11 12 database, N, is that it's O(kn), where K is a 13 constant. What does that indicate to you? 14 The constant -- if K is a constant, the 15 Α two equations you've written are equivalent, because 16 O(n) or order of, say, 2N is the same thing 17 18 mathematically. 19 Does it, in both instances, indicate that 0 20 the search time is on the order of linear? 21 Α At most linear. 22 Ο If all we know about a search is that its 23 search time compared to the size of the database 24 over which we're searching grows O(n) or (kn), do we 25 know that it's sublinear?

Page 20 We don't know because the notation is not 1 Α 2 refined enough to indicate that. You would have to use another notation. 3 What other notation? 4 \bigcirc 5 The theta of N notation. Ά 6 What's the "theta alpha notation"? Ο 7 Α "Theta of N" notation. Theta of N notation. 8 0 So if instead of big O you had written 9 Α theta, that would mean linear N. 10 11 Why don't you go ahead and write that down Ο for me on Exhibit 2005. 12 13 And what you've written there is, just for the record, something that looks like an H with a 14 circle around it, (n). And that's pronounced theta 15 of N? 16 17 It's capital letter theta. Greek letter. Α And it's pronounced "theta N"? 18 Q 19 А Theta of N. 20 Ο Theta of N. 21 Now, if we have something that's theta of 22 KN, what does that indicate? 23 Again, if K is a constant, like 2, there Α is no difference between theta of N and theta of KN. 24 25 They mean the same thing mathematically.

When we're assessing whether or not a 1 0 2 given search is a sublinear search or sublinear time search, do we determine it based upon whether or not 3 the search time grows compared to the size of the 4 5 query? 6 А You have said -- okay. We need to be specific here. 7 8 You say the search time. Okay. You're 9 looking at the search time as a function of -- now 10 this has to do with query; before you talked about 11 the size of the database. Which one is it? 12 Let me back up and ask you another couple Ο 13 of questions. When we're -- in this field when we're 14 talking about a -- using a search, what we're doing 15 is we're comparing a query or a pattern against a 16 database of data; is that right? 17 18 Α Yes. 19 And if we talk -- is it -- are there other Ο 20 words for "query" or "pattern"? What's the -- what's the best one to use? 21 "Query" is fine. One could -- could say 22 Α "probe" as well. 23 24 "Probe" or "query" or "pattern," they're 25 all synonymous in this context?

Yes. 1 A 2 In -- in looking at some of the prior art, 0 they refer to a -- trying -- having a song or a 3 melody that is unknown and then trying to determine 4 5 what that melody actually is. 6 You're familiar with that sort of prior 7 art? 8 Α Yes. Is the unknown melody the equivalent of 9 Ο the query or the pattern that we're searching for? 10 11 Α So the -- the -- what's submitted by the user is the query; what you are comparing it against 12 is -- is the database. So it --13 When you say "database," is that the same 14 15 thing as "dataset" in this context? 16 A Yes. 17 Now, if we're trying to determine whether Ο a given algorithm is sublinear or linear, do we 18 assume that the query size is fixed or does the 19 20 query size vary when we're trying to assess whether it's sublinear? 21 22 Α It depends on the problem considered, the 23 different flavors of these problems. 24 If we're trying to determine whether Ο something is sublinear as it's used in the claims of 25

the -- claims of the patents -- withdrawn. 1 2 If we're talking about the concept of sublinear search or sublinear time search as it's 3 used in the '237 patent, does that refer to a search 4 time that grows at a sublinear rate as we increase 5 6 the size of the pattern, or -- or does it refer to a search that increases at a sublinear rate as we 7 increase the size of the database? 8 9 Α Usually, the one that matters is the size of the database, because that's a big one. 10 When the -- in your definition that you 11 Ο set forth on page 19, where you said, "A sublinear 12 search means a search whose execution time has a 13 sublinear relationship to database size," you're 14 referring to "sublinear" as it's used in the '237 15 patent; is that right? 16 17 Α Let me check the '237 patent. What I gave in my Declaration is a general 18 19 definition of sublinear search. In the patent 20 here -- for instance, if you look at Claim 5 that 21 you -- we just discussed, sublinear time is used. 22 It does not say what the reference is. 23 Again, in those problems, the parameter 24 that's very big that's of concern is the size of the 25 database.

Page 24

1	
_	Q is it the case that in doing your analysis
2	to determine whether or not prior art anticipated,
3	you applied the definition that a sublinear search
4	or a sublinear time search was one whose execution
5	time has a sublinear relationship to the database
6	size?
7	A That is correct, yes.
8	Q Is that the correct definition that should
9	be applied, or are you applying the wrong
10	definition?
11	A In my opinion, this is the correct
12	definition to be used.
13	Q Would it be wrong to apply a definition
14	that said, "I'm going to determine if it's sublinear
15	based upon whether or not the search time grows
16	compared to the size of the query or the pattern?
17	A Mathematically, this could be done.
18	Whether it's relevant from an engineering point of
19	view is a different matter.
20	My opinion here is as an engineer. Okay?
21	The parameter that's big that's of concern is the
22	database size.
23	Q In trying to determine whether or not the
24	'237 patent is anticipated, is it your opinion that
25	the definition you've set forth in paragraph 53 is

		Page	25
1	the correct one?		
2	A That's the definition I have applied. And		
3	I, yes, believe it's correct. That's my opinion.		
4	Q Would it be wrong, then, to assess whether		
5	a search is sublinear by applying a definition that		
6	said, "It's sublinear if this execution time has a		
7	sublinear relationship to the size of the query or		
8	the pattern"?		
9	A It would not be very relevant. Again,		
10	mathematically, it can be done. Everything can be		
11	done. But it would not be relevant, from an		
12	engineering viewpoint, for an application like this.		
13	Q It wouldn't be relevant to the		
14	assessing the '237 claims; is that right?		
15	A In the field of database search in		
16	general and this includes the the patents		
17	we're discussing it's the database size that is		
18	the large number. And when you say "order of,"		
19	typically you refer to that.		
20	Q If we're trying to determine whether the		
21	'237 withdrawn.		
22	Let's assume somebody came along and said,		
23	"Listen, I'm going to assess the '237 patent, but		
24	I'm not going to look at whether or not this prior		
25	art scales based upon the size of the database; I'm		

		Page 20	6
1	going to look at whether it scales b as ed upon the		
2	size of the query or the pattern."		
3	Would they then be accurately assessing		
4	the '237 patent claims?		
5	A No. They would be looking at only one		
6	small view of the problem. They they could not		
7	look only at that. It's only a very partial view of		
8	the problem.		
9	Q Is it the case that for something to be		
10	withdrawn.		
11	Is it the case that for a search to be		
12	sublinear as it's used in the '237 patent, it's not		
13	enough for it to have execution time that is		
14	sublinear in relationship to the size of the		
15	pattern; it must also be sublinear in relationship		
16	to the size of the database?		
17	A When I read "sublinear" in, say, Claim 5		
18	of the patent, as we just did, I understand		
19	sublinear to mean in relation with the size of the		
20	database. It does not say anything about in		
21	relation with the size of the query.		
22	Q If we were doing withdrawn.		
23	If someone was doing an assessment		
24	withdrawn.		
25	Let's assume that the Patent Trial and		

		Page	27
1	Appeal Board was presented with prior art that		
2	presented a search that was linear with respect to		
3	the size of the database, but it was sublinear with		
4	respect to the size of the pattern.		
5	Would that prior art demonstrate a		
6	sublinear search as it's used in Claim 25?		
7	A People say it's a linear search, again,		
8	because it's in relation with the size of the		
9	database. And as you just said, that complexity is		
10	still linear; so people would say it is a linear		
11	search.		
12	Q It is not a sublinear search?		
13	A It's only sublinear in terms of the size		
14	of the query, which is generally not the		
15	parameter of the relevant parameter.		
16	Q Is it the case that if we had a piece of		
17	prior art that was linear with respect to the size		
18	of the database but sublinear with respect to the		
19	size of the query or the pattern, that that prior		
20	art would not teach a sublinear search as it's used		
21	in Claim 25?		
22	A Again, if one understands sublinear to be		
23	in terms in relation to the size of the database,		
24	that would be a a linear search.		
25	Q My question wasn't "if one understands"; I		

		Page 28
1	want to get your understanding of Claim 25. So you	
2	still haven't answered my question. I'll ask you	
3	again.	
4	Let's assume we've got a piece of prior	
5	art that scales at a sublinear relationship with the	
6	size of the pattern or query but it scales at a	
7	linear relationship with the size of the database	
8	that's being searched.	
9	Would that prior art demonstrate or	
10	disclose a sublinear search as it's used in the	
11	claims of the '237 patent?	
12	A No. Again, because my understanding is	
13	the claims of the '237 patent, whenever there's	
14	mention of "sublinear," it means in terms of the	
15	database size. It does not say it explicitly; it's	
16	my inference based on my knowledge and my expertise.	
17	Q Let's assume we have a search that's	
18	execution time is O(mn), where M means the size of	
19	the query, N means the size of the database or	
20	dataset that we're searching over.	
21	What does that tell us?	
22	A Well, it means that the search time,	
23	<pre>i(m)n, grows at most linearly.</pre>	
24	Q Is it the case that this would be a	
25	sublinear search as it's used in the '237 patent?	

Page 29 1 It says, again, it's at most linear A No. 2 in terms of M times N. 3 Let's assume we have a -- withdrawn. 0 What I've tried to write there -- and see 4 5 if I wrote it correctly -- is we've got a search, 6 and the search time is O(f(m)n). Does that -- do you understand what that 7 8 refers to? 9 Ά Yes. What would that indicate? 10 Ο 11 Well, that the search time, as a function Α of that quantity in parentheses, grows at most 12 13 linearly. Is it the case that if N, in that example, 14 0 refers to the size of the database, do we have, 15 16 then, a sublinear search? Well, you have to tell me if M grows too, 17 Α or if it's a constant like in your -- in your 18 19 previous example? 20 0 Let's assume that M is the size of the 21 query. 22 Α Uh-huh. 23 M, as in Mary. And that N, as in Nancy, Q is the size of the database. 24 25 Α Okay.

1 Q In that instance, does this describe a 2 search that has -- that is -- has sublinear 3 execution time when compared to the size of the 4 database?

5 A Your question is incomplete. There's an 6 assumption you need to specify. Does M grow, or 7 does N grow, or is it both?

8 Q Well, my question is if we're presented 9 with this information, and we want to know is this 10 search sublinear or linear with respect to the size 11 of the database, where N is the size of the 12 database, does that tell us?

13 A No. Because you have not told me how 14 either M or N grows. The product of f(m)n has to 15 grow. For that to grow, either M or N has to grow, 16 or both. But you need to tell me which one.

17 Q If N refers to the size of the database, 18 and we're trying to assess whether that describes a 19 search that is sublinear with respect to the size of 20 the database, can we -- what does that tell us?

A This tells us that the search time grows at most linearly in terms of the product f(m)n. You have not told me whether it is M that grows or N that grows. The product has to grow, but there are different ways in which it can grow. N alone can

1	grow and M is fixed, or M can grow and N grows.
2	So the answer depends on your assumption.
3	You need to specify your assumptions.
4	Q If we're trying to determine or assess
5	whether or not this search is sublinear with respect
6	to database size, and if N, as in Nancy, refers to
7	database size, then would that indicate that we're
8	going to be assessing this assuming that N grows and
9	that M is fixed?
10	A It depends on the problem. In some
11	problems, indeed, M could be fixed and N grows.
12	That's a a possibility.
13	Q Well, my question is if we're trying to
14	determine whether or not a given search is sublinear
15	with respect to the size of the database, that means
16	that we're going to determine execution time
17	compared to the growth of the database, N; right?
18	A Yes.
19	Q If that's the case when we're presented
20	with this information, then is the assumption that M
21	is fixed if we're trying to determine whether it's
22	sublinear with respect to the growth of N?
23	A Different applications could have
24	different M. Some applications could have fixed M;
25	other applications could have M grow like N. It

1 depends on the application.

2 If we're trying to -- suppose I present 0 you with an algorithm, and I say to you, "I want to 3 know, in your opinion, does this describe a linear 4 or a sublinear algorithm with respect to the 5 database time?" 6 7 And T --8 Α "Size," you mean. 9 Ο Right. With respect to the database size. And I present -- let's take Algorithm 1, 10 2, 3, 4, the one that says "O(mn)." I present that 11 12 to you. 13 Α Yes. Do you have an opinion? 14 Q 15 Α Can you repeat your question. 16 Yeah. If -- so just to be clear, in fact, Ο I'm going to take Exhibit 2005, and just for 17 clarity, I'm going to put a number next to each of 18 19 these formulas we've written down. Starting at the 20 top, it will be 1, 2, 3, 4, 5. Let's take a look at Formula Number 4. 21 22 Assume you're presented that information about a 23 given search. And the question is -- withdrawn. 24 Assume you're given number -- Formula Number 4 and told that M, as in mother, refers to 25

the size of the query; N, as in Nancy, refers to the 1 size of the dataset that we're searching over. 2 3 And you're asked the question, "Does that 4 tell us anything about whether or not the search is sublinear with respect to the size of the database?" 5 6 А I don't have enough information to answer It's really exactly like if you told me, "Ten 7 this. 8 is the sum of two numbers; tell me which ones." 9 Ο If we know that M refers to the size of the query and N refers to the size of the database, 10 11 and we're interested in whether or not the -- a 12 search is sublinear with respect to the size of the 13 database, does that tell us that it -- with respect to the size of the database -- that it grows on the 14 order of N, as in Nancy? 15 M and N could be related. You have not 16 Α 17 defined the relationship between them. If M is fixed, there's one answer, and -- which I've given 18 19 earlier -- it is: The growth is at most linear. 20 But if M grows with N as well, then the answer is different. 21 22 Ο Let's -- I want you to assume that M refers to the size of the query, N refers to the 23 24 size of the database, and that there is no 25 relationship between them except that N is greater

Page 34 The size of the database is greater than M. 1 than M. 2 Okay. So when you say there's no Α relationship, do you assume that M is fixed? 3 4 0 Well, if we're trying to answer this 5 question, is that the assumption that should be 6 made? 7 Α The way you have said it, mathematically, 8 to suggest M is fixed. So I want to make sure we're 9 on the same page. 10 Okay. What about the way I've said it 0 11 suggests that M is fixed? 12 Because you said there's no relation Α 13 between them. So that suggests to me that if one -say N increases, M does not because it's not 14 15 related. That's my assumption from what you said. 16 Okay. Let's assume they're not related. 0 17 In other words, were -- is that the typical problem we're facing, is that we've got a 18 19 database of a certain size that may change, and we've got different queries of different lengths, 20 21 whether the -- the query length is not going to 22 affect the database size in a typical problem --23 There may be a relationship. Α 24 It's possible? 0 25 Α Depends on the problem.

In the typical cases, is it that they do 1 0 2 not have a relationship? 3 Α I've encountered both types of problems. Well, the question isn't whether you've 4 Ο encountered them. 5 6 What's typical? Well, both are typical, I would say. 7 Α Ιt 8 depends on the problem. 9 Ο Okay. Now, let's assume that we have a -a problem we're dealing with where the size of the 10 11 query and the size of the dataset are unrelated. 12 And you're presented with the information 13 that's in Formula 4, that the search time is on the order of M, as in mother, times N, as in Nancy, 14 where M refers to the size of the query, N refers to 15 the size of the data set? 16 17 What information does that tell you about 18 whether it's linear or sublinear? 19 So based on your assumptions that you laid А 20 out, I treat M as a fixed number. Then the answer 21 is the same I gave earlier: It would tell me that 22 the search time is at most linear in N, as Nancy. 23 Let's assume we've got a search that's 0 24 O(f(m)n), where M and N are unrelated. What does 25 that -- where N refers to the size of the database.

		Page 36
1	What information does that tell us about	
2	whether it's linear or sublinear?	
3	A Same answer.	
4	Q Which is what?	
5	A That, again, it would be the search	
6	time would be at most linear in N.	
7	Q Linear as to the size of the dataset that	
8	we're searching over?	
9	A Exactly. Yes. And that's because you	
10	have treated M as fixed. So whether it's (m) or	
11	f(m) that appears in the equation is irrelevant.	
12	Q I've written down Equation or Formula	
13	Number 6, which I'm going to read it as on the order	
14	of N, as in Nancy, times log of M; is that right?	
15	A Yes.	
16	Q Let's again assume that N refers to the	
17	size of the database, M refers to the size of the	
18	query.	
19	Does that if we have a withdrawn.	
20	If we have a search that is described as	
21	set forth in Formula 6, where N refers to the size	
22	of the database, what does that tell us about	
23	whether it's linear or sublinear?	
24	A Same answer as previously. You have	
25	replaced f(m) with log(m). It's just a particular	
Page 37 1 function, f(m). So that would tell me that search 2 time is at most linear in terms of N. 3 0 If you're presented with that, does that 4 tell you that we have a sublinear search? 5 A In terms of N, yes. 6 0 In terms of --Sorry. Let me rephrase this. 7 A 8 It's at most linear. 9 0 Does that tell us that we have a sublinear 10 search? 11 A It does not tell me that, because of the 12 meaning of the order of notation. It says, at most, 13 linearly. 14 Let me ask you a different problem. Q 15 Let's assume we have a search algorithm, and what it does, it is able to perform its 16 search -- withdrawn. 17 18 Let's assume we've got a search algorithm, 19 and we're trying to take a pattern or query and see 20 if it matches any portion of a dataset. And in that 21 process, our particular algorithm operates such that 22 it doesn't need to look at every single character in 23 the dataset. 24 Are you familiar with algorithms of that 25 sort?

1 Α Yes. 2 Knowing just that information and no more, Ο does that tell you one way or the other whether it's 3 linear or sublinear? 4 5 No, it does not. Α 6 Why not? Ο 7 Α Because you have -- when you tell me it 8 does not look at every character, you don't tell 9 me -- you know, does it look at only half the 10 characters? Does it look at the square root of 11 number of characters? 12 So many possibilities. You need to 13 specify that. If it's the case that it looks at a 14 Ο 15 fraction of the characters, one -- one out of eight, one half, something like that -- does that tell you 16 whether or not the algorithm is sublinear? 17 18 Α If it's a fixed fraction -- for instance, 19 you tell me one eighth -- so if the algorithm looks 20 at one eighth of the number, if it looks at one 21 eighth of the size of the dataset, that would be 22 linear. Again, as the dataset -- as the data size goes to infinity, if you keep looking at one eighth, 23 24 it would be a linear relationship. It's one eighth 25 of M.

Page 39 It would be something like Formula 1 Ο Number 2, O(kn)? 2 No. Because Formula Number 2 uses the 3 Α order of notation; I would need to use the theta of 4 5 N notation. 6 So you would say that this one is not just 0 7 O(n), it would actually be --8 Α It behaves as a constant times N. 9 Ο And that would be a linear relationship; right? 10 11 Α Because you assume -- you look at, say, one eighth, you -- your calculation involves one 12 13 eighth of the database. Why don't you turn to page 20 of your 14 Ο Declaration. 15 Yes. Yes. 16 Α On page 20, this is where you've got the 17 Ο chart that explains linear search versus sublinear 18 search; right? 19 20 Right. Α 21 Q If we've got a search and what we know 22 about it is that it looks at a constant fraction of 23 the characters in the dataset, is that going to 24 be -- if we were to plot it -- one that gives us a 25 straight line like you plotted there?

		Page
1	A Well, my charts, my plots, only the	
2	horizontal axis is the number of entries in the	
3	database. So it says nothing about how many samples	
4	I'm evaluating for each entry.	
5	Q All right. Let's assume we've we've	
6	got a chart let's broaden your your definition	
7	here.	
8	Let's assume you're plotting search time	
9	versus size of a dataset. Okay?	
10	A Okay.	
11	Q If it's linear versus sublinear, we're	
12	still going to plot the same thing you've plotted	
13	there; is that right?	
14	A Yes.	
15	Q Now, let's assume we also know that our	
16	particular search algorithm examines a fraction of	
17	the characters in the dataset. Is that and that	
18	that fraction is constant over time as the size of	
19	the dataset increases.	
20	Is it the case, then, that that is going	
21	to be a linear or sublinear search?	
22	A It would be at least linear because,	
23	again, your assumptions are not completely	
24	specified. The fact that it evaluates a constant	
25	fraction means the complexity is at least linear.	

40

Page 41 1 And it could be worse? 0 2 Yes. Because it depends on the work you Α do with those samples. It might be that the 3 algorithm is very complex. And as complexity, N 4 5 square. 6 Would that tell us that it's definitely 0 7 not sublinear? 8 Α Yeah, N square is definitely not sublinear. 9 10 But if we knew that the algorithm 0 11 evaluates a constant fraction of the characters, does that tell us that it's not sublinear? 12 13 Α Yes. Why is that? 14 Q Well, because the work involved includes 15 Α evaluating a fixed fraction of N. So then, by 16 definition, this cannot be sublinear. 17 18 Why is that? Ο 19 Because you work, let's say, at least n/8, Α 20 to take your example from earlier. To have a sublinear relationship, it would need some function 21 22 that grows less than linearly. So n/8 grows linearly. 23 24 Are you familiar with a search algorithm 0 25 known as the Boyer-Moore algorithm?

Page 42 1 Α Yes. 2 When did you first encounter that? Q Hard to say. I -- I don't remember. 3 Α 4 Ο Many years ago? 5 Α Probably, yes. 6 Is the Boyer-Moore algorithm one that's 0 7 been well studied, or is it something that people know very little about? 8 It's a pretty well-known algorithm. 9 Α Is it one that numerous peer-reviewed 10 Ο 11 papers have been written describing the performance 12 of the Boyer-Moore algorithm? 13 Many papers have been written, as far as I Α know, discussing the paper and improving it, yes. 14 15 If we take the basic Boyer-Moore --Ο withdrawn. 16 17 When you say "improving it," there are 18 variations of the Boyer-Moore algorithm; is that 19 right? 20 Α Yes. Many. 21 Q Where people have taken it and modified it 22 in various ways? 23 Or modified the assumptions. Α 24 Let's take the basic Boyer-Moore Ο algorithm. 25

Are -- have you done any analysis 1 2 yourself, independently, to determine whether or not the Boyer-Moore algorithm is an algorithm that is 3 sublinear with respect to the size of the database 4 5 being searched? The Boyer-Moore algorithm says nothing 6 Α 7 about a database. It's a very basic problem that 8 involves finding a pattern in a string. You know, 9 that algorithm could be used in a variety of 10 contexts, including database searching. 11 Is the -- is the Boyer-Moore algorithm one 0 12 that is sublinear with respect to the size of the 13 dataset being searched? The Boyer-Moore -- let me just review 14 Α this. Can you point me in my Declaration where this 15 was discussed. 16 17 Well, I'll get to that in a second --0 18 Α Fine. 19 -- let's start -- let's start with your --Ο 20 what you recall. I don't recall the constants in 21 Α 22 Boyer-Moore. I would have to check them in my 23 Declaration. 24 When you say "the constants," what do you Ο mean by "the constants"? 25

Well, the Boyer-Moore algorithm presents 1 Α 2 an efficient search algorithm, and you have a average-case performance; there's also worst-case 3 4 performance. And it tries to precisely determine 5 what that performance is. The "order of" is viewed as somewhat 6 7 imprecise. It does not tell me what the constants 8 could be. So 1/8n or 10n are both O(n). But the 9 constants are the same: 1/8 or 10. 10 In preparing your Declaration, you -- you 0 made some comments about the Boyer-Moore algorithm, 11 12 is that right, in your Declaration? 13 Α Yes. All right. When you made those comments, 14 0 did you do that from your memory, or did you do some 15 16 research to determine the performance of the 17 Boyer-Moore algorithm? 18 Α I don't recall. I probably did it from 19 memory, yeah. 20 Can you describe generally how the 21 Boyer-Moore algorithm functions, what it does. 22 Yeah. So if you have too much string --23 let's say the word "second." If you want to find 24 that string in, say, a page of text or in a book, 25 there's a straightforward way to do it, which most



1 That could not be. A No. 2 Why not? 0 Well, the larger your database, or in this 3 A 4 case, the page of text in the example I gave, the 5 more work you have to do. So it could not possibly 6 go down. 7 Ο Could it be the case that based on the way 8 Boyer-Moore operates, that the search time would be 9 sublinear such that as we continue to increase the size of the database, the proportion of time that we 10 11 needed would go down? 12 Again, sublinear in what -- I need to Α 13 review -- there are different ways to state the complexity. I need to review the way it was done in 14 my Declaration. 15 16 When you say the way it was done in your Ο Declaration, what are you referring to? 17 18 Well, Boyer-Moore was discussed in my Α 19 Declaration. Again, there are two quantities of 20 interest. One is the size of the pattern you are 21 trying to match, and the other one is the length of 22 the string, okay, of the text in the example. 23 All right. Well, I'm going to get you 0 24 your Declaration. In fact, why don't you just close 25 it. I don't want you to get confused here.

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A Pardon?

1

2 Q I'm going to have you look at it in a 3 minute. I need to -- you have to focus on my 4 questions first.

5 When you did your analysis that you put in 6 your Declaration, did you go to some basic sources 7 to see what it -- what the published results were 8 for the performance of the Boyer-Moore algorithm?

9 A I verified them. I have, again, some 10 recollection of what the complexity -- both the 11 worst-case and the average-case complexity of 12 Boyer-Moore are, and I verified them, yes.

Q Now, when you -- did you look at Boyer-Moore's original paper describing the algorithm?

A Yes. That's my recollection, at least. Q Did you look at some of the other well-known papers that assess the performance of the Boyer-Moore algorithm or just -- just the original Boyer-Moore paper?

A Well, the performance was already assessed in the paper itself. So follow-up papers looked at the variations of the problem. They referred to Boyer-Moore because it's a golden standard.

25 Q Did you -- do you recall seeing any paper

1 that said that -- withdrawn.

2	Do you recall seeing any paper that
3	presented an analysis, either theoretical or
4	experimental, that showed that the Boyer-Moore
5	algorithm was sublinear with respect to the size of
6	the dataset being searched?
7	A Again, performance of this algorithm is
8	given in terms of two quantities. I would have to
9	review I don't remember the the exact formula.
10	I would have to review it. I don't know it offhand.
11	Q When you did your analysis
12	A Right.
13	Q in preparing your Declaration, did you
14	see any source, any published source that presented
15	either theoretical results that is a mathematical
16	calculation or actual experimental results that
17	showed that the Boyer-Moore algorithm was sublinear
18	with respect to the size of the dataset being
19	searched?
20	MR. ELACQUA: Asked and answered.
21	THE WITNESS: Yeah. Boyer-Moore gives those
22	results. As I've just said, there's a formula which
23	apparently you don't want me to check. I don't
24	remember the formula by heart, okay. They give a
25	formula. The time complexity in terms of these two

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1 parameters.

2 BY MR. DOVEL:

3 Q When you say "these two parameters,"
4 you're talking about the query and the database
5 size; is that right?

6 A The string -- the long string in which we 7 try to find the pattern.

8 Q Okay. But my question is when you did 9 your work, did you see an actual paper that 10 presented either experimental results or a 11 theoretical calculation?

12 A The theoretical calculation was done by 13 Boyer-Moore. Other works have used it, for 14 instance, Iwamura, Ghias. This algorithm has been 15 used by -- by many people.

16 Q Are you telling me that when you prepared 17 your Declaration, you looked at the original 18 Boyer-Moore paper?

A I don't recall. I think I did. I don't recall if I looked at original paper or a reference that gave Boyer-Moore. There are different ways to obtain the formula. You can, of course, look at the original paper or you can look at a reference that gives that formula.

25 Q Okay.

Page 50 1 I don't remember which one I did. Α MR. DOVEL: Okay. Let's go ahead and take a 2 break, and we will return in about five minutes. 3 THE VIDEOGRAPHER: We're off the record at 4 5 9:58 AM. 6 (Off the record.) 7 THE VIDEOGRAPHER: We are back on the record 8 at 10:11 AM. MR. DOVEL: I'm holding a document entitled "A 9 Fast String Searching Algorithm." It's by Boyer and 10 This will be Exhibit Number 2006. 11 Moore. (Exhibit 2006 was marked for identification 12 13 by the court reporter and is attached hereto.) 14 15 BY MR. DOVEL: 16 I've placed Exhibit 2006 in front of the Ο witness. 17 18 Dr. Moulin, do you recognize this paper 19 generally as the paper by Boyer and Moore that published the Boyer-Moore algorithm? 20 21 Α Yes. 22 0 I'm going to look at several parts of this 23 with you, but I just want to look at the abstract. 24 One of the things it says in the abstract is, "The worst-case behavior of the algorithm is 25

linear in i plus patlen." 1 2 Do you see that? Yes. 3 Α "Patlen," that refers to the length of the 4 Ο 5 pattern or length of the query; is that right? 6 А I assume so. Seeing this, I'm -- I have not read the paper itself. I'm, again, familiar 7 8 with the result; I have seen the result quoted in 9 other papers. So I would have to read the notation. 10 But it seems straightforward. 11 Well, if we look at the introduction on 0 12 page 1, the first sentence says, "Suppose that pat 13 is a string of length patlen." 14 Do you see that? 15 Α Yes. 16 Is it your understanding, then, that Ο patlen is going to correspond to the length of the 17 18 query? 19 Α Yes. 20 Now, if we look in the introduction, down Ο 21 about paragraph 1, 2, 3, you see a sentence that 22 says, "We now present a search algorithm which is 23 usually 'sublinear.'" 24 Do you see that? 25 Α Yes.

Page 52 And then he goes on to describe what he 1 Ο means by "sublinear." 2 3 Do you see that? 4 Α Yes. Again, I would have to read it 5 carefully. 6 Is what Boyer and Moore are describing 0 here when they used the term "sublinear" is an 7 8 algorithm that is sublinear with respect to the 9 length of the pattern or query? 10 I would have to read this. Again, this is Α not a paper I have read before. I'm familiar with 11 12 the results, but I have to read the whole paragraph. 13 You have not read this paper before? 0 I am familiar with the results, but I have 14 Α 15 not read the entire paper before. 16 Have you read any portion of the paper Ο 17 before? 18 I'm -- the results, yes. Α 19 Have you read any portion of the paper Ο 20 before? 21 Α I -- I might have seen -- again, I've seen before -- I'm sure I did not read it completely. 22 23 In preparing your Declaration, did you 0 24 pull up a copy of the Boyer-Moore article to see 25 what it said about the performance of the

Boyer-Moore algorithm? 1 2 Α I looked at the results. That does not 3 mean that I read the paper completely. 4 Ο So I want to get an answer to my question. Did you -- when you say you looked at the 5 6 results, did you look at portions of this paper in 7 preparing your Declaration? I looked at the main results. So if 8 Α 9 that's what you call a portion, yes. I did not read the complete paper. 10 11 When you said you looked at the main 0 12 result, what page was that on? The main results, I don't remember which 13 Α page it's on. The main results is given already in 14 the -- in the abstract, and it's stated more 15 precisely further down in the paper. 16 17 Okay. Let's take a look at what it says 0 18 in the abstract. 19 Does the abstract state that the 20 Boyer-Moore algorithm is sublinear with respect to 21 the size of a database? 22 There's no database in Boyer-Moore. A 23 Does Boyer-Moore -- does the abstract 0 24 state that the Boyer-Moore algorithm is sublinear with respect to the size of the dataset being 25

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1 searched?

A There's two notions of complexity. One, as I said before, is worst case, and the other one is average case.

5 So if you look at worst-case behavior of 6 the algorithm, which is at the end of the abstract, 7 "The worst-case behavior of the algorithm is linear 8 in i plus patlen."

9 Then earlier, there is somewhere a 10 discussion about the average performance. Okay. 11 Here. So it's a few sentences above. On average, 12 the algorithm executes fewer than i plus patlen 13 machine instructions. So you need to separate the 14 two.

15 Q Well, let's take both.

16 Did either one of those address -17 withdrawn.

18 The abstract, what it talks about is the 19 behavior of the algorithm with respect to the length 20 of the pattern; right?

A The sum. There's i, and there's patlen.
Q And what does i represent?
A So i represents, in their notation, the
location of the first occurrence of the pattern in
the string.

What does the -- when we -- if we know 1 0 2 that an algorithm -- withdrawn. What does the abstract indicate with --3 withdrawn. 4 5 Does the abstract indicate that -- or have 6 comments about the behavior or performance of the 7 algorithm with respect to the pattern length? 8 Α Yes. Because both -- whether you look at 9 average or worst-case performance, it's characterized in terms of i and patlen. 10 11 Does the abstract have any comments about Ο 12 the performance of the Boyer-Moore algorithm with 13 respect to the size of the dataset being searched? 14 Implicitly, yes. Α 15 Ο What's the implicit? 16 Well, because this location prior to i can Α vary, it could be 1, okay, this i could be the very 17 first character in the string, or it could be the 18 19 last possible location. 20 And what does that tell us about whether Ο 21 it's sublinear with respect to the size of the 22 dataset? 23 Well, so if you view patlen as being a Α 24 fixed number, say 10 -- you're trying to match a word -- and you have a string of length, say N, then 25

the largest possible value of i is n-10. Okay? 1 So it is a function of N. 2 3 Q Is it the case that the average value of i is going to be n/2? 4 5 Α Yes. 6 Approximately? Ο 7 Α Yes. 8 Ο Is it the case that if we have -- let's take the worst-case behavior. 9 10 When it says, "The worst-case behavior of 11 the algorithm is linear in i plus patlen," that's a statement that if we put it in big O notation, that 12 it would be O(n+m); is that right? 13 Yes. 14 Α I'm going to write that down. Number 7. 15 Q 16 And in Number 7, N would correspond to the size of the dataset, M to the length of the pattern; 17 is that right? 18 19 Α Yes. Is it the case that what Boyer-Moore tells 20 Ο 21 us in the abstract, if we look at the upper bound 22 for the behavior, it's O(n+m); is that right? 23 What do you call "the upper bound"? Α The worst-case behavior? 24 25 Yes. 0

Page 57 1 Α Yes. 2 Is another way for that -- when we're Ο talking about worst-case behavior, is that also 3 referred to as "the upper bound"? 4 Well, an upper bound is not unique. 5 Α It's 6 "an upper bound." Is it the case that -- withdrawn. 7 Ο 8 Now, so if we look at the -- look at that 9 statement, does that suggest that the Boyer-Moore algorithm is sublinear with respect to the size of 10 11 the dataset? 12 This is -- you're looking at the Ά worst-case behavior. 13 Yes. 14 Ο 15 So the worst-case behavior is linear. Α Would that be sublinear? 16 Ο 17 The worst-case behavior is linear in А No. i plus patlen. Now, the worst case, again, is when 18 19 i is N minus patlen, that would be linear N, the 20 worst case. Is there anything in the -- in the 21 Q 22 abstract that tells you that the Boyer-Moore algorithm is sublinear with respect to the size of 23 24 the dataset being searched? 25 Α Let me read the abstract again.

Page 58 So the way, in that paper, they have 1 2 characterized performance is in terms of i and patlen. i is a number that ranges from 1 to a value 3 close to N. Okay. So it does not give the 4 performance directly in terms of N; it's in terms of 5 6 i and patlen. 7 Ο When you read the abstract to the 8 Boyer-Moore algorithm paper, does it suggest that 9 the Boyer-Moore algorithm is sublinear with respect to the size of the dataset? 10 11 With respect to the size of the string, Α 12 the dataset? 13 Yes. Ο So in the worst case, no. It's linear in 14 Ά 15 the worst case. Does it have any suggestion that it's 16 Ο sublinear with respect to the size of the dataset? 17 18 Well, for instance, if i was the square Α 19 root of N, then it would be sublinear. 20 Well, that's not my -- question is "if." Ο 21 My question is this: Is it the case that 22 if you look at the abstract here, does the abstract provide any indication that the Boyer-Moore 23 24 algorithm is sublinear with respect to the size of 25 the dataset?

Page 59 The abstract does not give performance --1 Α 2 it gives performance in terms of i plus patlen, not directly in terms of N. So this i could be as small 3 4 as 1 or as big as N minus patlen. 5 You haven't answered my question. 0 6 Does the abstract provide any indication 7 that the Boyer-Moore algorithm is sublinear with 8 respect to the size of the dataset being searched? 9 A No. 10 MR. ELACQUA: Object. Asked and answered. 11 BY MR. DOVEL: 12 What was your answer? Ο 13 Α No. Why not? 14 Q 15 Α Because the abstract talks about something else. It talks about i and patlen. 16 17 And because it talks about i and patlen, Ο what it tells you is that the expected -- withdrawn. 18 19 As you understand i, i is a function of N; 20 right? 21 Α No. i is a number anywhere between 1 and 22 N minus patlen. As N grows, does -- withdrawn. 23 0 24 Now, if we look at -- you've said that you 25 looked at the main results of Boyer-Moore to

Page 60 determine -- withdrawn. 1 2 You said earlier that you looked at the 3 main results in this paper, which is Exhibit 2006, to determine the -- what it had to say about the 4 5 performance of the Boyer-Moore algorithm. 6 Did you look someplace other than the 7 abstract or just the abstract? 8 Α I don't recall where I looked exactly. Ι know I looked at other references as well. 9 Other references. 10 0 11 Other than this paper? 12 Α Yes. 13 Okay. I'm talking about this paper. Ο I don't recall where exactly I -- I read 14 Α 15 the results we're discussing. These are very well-known results. Again, I've seen -- I've seen 16 those results before. 17 When you say the "results," the 18 Ο 19 performance of the Boyer-Moore algorithm is well 20 known? 21 Α Yes. It's a well-established paper in 22 1977. 23 Well-known to people in your field; right? 0 24 Well-known to many people. Α 25 How about to you? Was the performance of Q

the Boyer-Moore algorithm well known to you? 1 I knew it was much faster than brute 2 Α force. Again, the exact order of and constants, I 3 4 have read them a while ago. I refreshed my memory 5 for this case. But it's a well-known way to improve 6 over brute-force algorithms. 7 Q Having refreshed your memory, what is your 8 memory of what the performance of the Boyer-Moore 9 algorithm is? 10 Well, we've just discussed it. Α 11 So you look at worst-case complexity; you 12 look at average performance, average complexity. 13 There are two quantities of interest. One is the length of the pattern, called patlen here in this 14 paper, and there is the location, the location of 15 16 the pattern in the string, which ranges from 1 to N 17 minus patlen. 18 Are you familiar with any analysis of the 19 Boyer-Moore algorithm with respect to the size of 20 the dataset being searched? 21 It's described here. So, again, this i, A 22 if you look at the worst case, i is N minus patlen, 23 then you obtain it. As I said, it will be a linear 24 relationship. 25 As one of ordinary skill in the art, if 0

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1	you read the Boyer-Moore article, would you come to
2	the conclusion that what it says about the time
3	complexity of the Boyer-Moore algorithm is that it
4	would scale execution time in a linear relationship
5	worst case, compared to the size of the dataset
6	being searched?
7	A Yes. And also, it is known to be much
8	faster than brute force. A person of ordinary skill
9	in the art would know that.
10	Q The fact that it's faster than brute force
11	does not tell you that it's sublinear; right?
12	A No.
13	Q In fact, what this paper tells you based
14	on the analysis that's here is that it's on the
15	order of linear; right?
16	A In the worst case, yes.
17	Q Now, did you in your Declaration, you
18	didn't mention the Boyer-Moore paper, which says
19	that the Boyer-Moore algorithm has a performance
20	compared to the size of the database that's on the
21	order of linear; is that right?
22	A I need to check where this is discussed in
23	my Declaration. Can you point me to the right page.
24	Q I think I can. Give me a minute.
25	A Sure.

		Page	63
1	Q Take a look at page 27 in your		
2	Declaration. Stick with the right page here.		
3	In paragraph 72, you mention the		
4	Boyer-Moore algorithm.		
5	Do you see that?		
6	A Yes.		
7	Q In your Declaration, you didn't mention		
8	that in the Boyer-Moore paper, that Boyer-Moore		
9	described the algorithm as having a linear		
10	relationship with respect to the size of the		
11	database rather than sublinear; is that true?		
12	A Can you repeat your question. Sorry.		
13	Q Yeah. In your Declaration		
14	A Yes.		
15	Q when you discussed the Boyer-Moore		
16	algorithm at paragraph 72, do you mention the		
17	Boyer-Moore paper, which states that the Boyer-Moore		
18	algorithm has a linear relationship rather than a		
19	sublinear relationship with respect to the size of		
20	the database?		
21	A Well, I quoted Exhibit 1017, which reads,		
22	"On the average, the Boyer" "the algorithm has a		
23	sublinear behavior." So reference Exhibit 1017		
24	was I have to remember what it was.		
25	Q That's a reference by Raita.		

By --1 Α 2 Raita, R-a-i-t-a. Ο 3 Α Okay. 4 Ο I need an answer to my question. 5 So as I just read -- so -- I quoted a Α 6 passage from that exhibit that reads, "On the 7 average, the Boyer-Moore algorithm has a sublinear behavior." That's all I did. 8 9 I need an answer to my question. 0 Sorry. Can you say it again. 10 Α 11 Sure. In paragraph 72, when you discussed Ο 12 the Boyer-Moore algorithm and its performance, did 13 you mention the Boyer-Moore paper that you had reviewed which described the performance as linear 14 rather than sublinear? 15 16 I quoted another paper. That's all I did. Α 17 Did you mention the Boyer-Moore paper? Ο Α I mentioned Exhibit 1017 as the reference. 18 19 I mentioned -- and that sentence discusses the 20 Boyer-Moore algorithm, yes. 21 Q Not the algorithm. 22 Did you mention the Boyer-Moore paper? 23 Not in this paragraph 72. As you told me, Α 24 Exhibit 1017 is another paper. This paragraph does 25 not quote the Boyer-Moore paper.

Page 65 In paragraph 72, did you mention the 1 0 2 results that are found in the Boyer-Moore paper that describe the algorithm as linear rather than 3 sublinear? 4 5 In that paragraph, the only discussion of Α 6 sublinearity is a quote from another paper, which is 7 Exhibit 1017. 8 Ο From that, I can infer the answer to my 9 question. I need you to answer it. 10 I'm sorry. Can you repeat the precise Α 11 question. 12 In paragraph 72 in your Declaration --Ο 13 Α Yes. -- when you discuss the Boyer-Moore 14 Ο algorithm and its performance, did you also mention 15 that the Boyer-Moore paper described the performance 16 as linear? 17 18 Not in that paragraph, no. Α 19 Why not? 0 20 I'm just reading the five lines here, and Α it does not say that. 21 22 Ο Why didn't you put it in here? 23 I don't remember why I didn't mention it. Α 24 Did you want to conceal it from the Patent 0 Trial and Appeal Board? 25

		Page
1	A Of course not.	
2	Q Then why not put it in here?	
3	A Because it may not have been truly	
4	relevant. The whole relevance of Boyer-Moore is to	
5	indicate one way in which sublinearity can be	
6	obtained. There are many ways. So this is just one	
7	way in which it can be obtained.	
8	Q You are is it withdrawn.	
9	In paragraph 72, are you representing to	
10	the Board that it's your understanding that the	
11	Boyer-Moore algorithm has a sublinear behavior with	
12	respect to the size of the dataset?	
13	A No. This is just a quote of another paper	
14	discussing Boyer-Moore. This Boyer-Moore algorithm	
15	has been used in a variety of contexts, including,	
16	of course, content recognition. I'm simply quoting	
17	from another paper here. I'm not presenting	
18	anything about what you asked.	
19	Q Well, you say, "It is my opinion that	
20	Iwamura further teaches how the search can be	
21	<pre>sublinear"; right?</pre>	
22	A Let me just read again.	
23	That's right. So	
24	Q When you used the word "sublinear" there,	
25	are you using it to mean sublinear with respect to	

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the size of the dataset? 1 It is -- okay. The search can be 2 Α sublinear in the size of the database. There are 3 many ways for which it is sublinear in the size of 4 5 the database. I actually want to supplement this 6 opinion. I said, "For example, this is just one 7 way." I want to supplement my opinion, if you wish. 8 0 Well, I want to an understanding of what 9 vou wrote here --10 Right. Α 11 -- and what you were trying to tell the Ο 12 Board. 13 А Right. You understood the Board was going to read 14 0 this as actual sworn testimony by you; right? 15 16 Α Yes. 17 And when you wrote this, were you trying 0 18 to convey to the Board that the Boyer-Moore 19 algorithm is one that, if you use it, it's sublinear 20 with respect to the size of the database? 21 A No. No. 22 0 If one were to read this -- withdrawn. 23 Is it your opinion that the Boyer-Moore 24 algorithm is sublinear with respect to the size of 25 the database?

It does not say anything, because 1 Α 2 Boyer-Moore is kind of a piece in a puzzle; right? It's used to find a pattern in a string. 3 4 If you want to apply it to a larger problem like 5 database searching, as Iwamura has done, there's a variety of ways to use that. I did not even do the 6 7 analysis that Iwamura may have done. Because 8 there's a variety of ways to obtain sublinearity. 9 0 Is it your opinion that, using the Boyer-Moore algorithm, that it is a search technique 10 11 that is sublinear with respect to size of the 12 dataset being searched? 13 Α If you look at the basic Boyer-Moore problem, which is finding a pattern in the string, 14 the worst-case behavior is linear in the size of 15 16 the -- of the string. 17 Is it your opinion that the Boyer-Moore Ο algorithm is sublinear with respect to the size of 18 19 the dataset being searched? 20 MR. ELACOUA: Asked and answered. 21 THE WITNESS: I cannot answer the question. 22 If you read the Boyer-Moore paper, as we have discussed, the parameters are i and patlen. 23 24 BY MR. DOVEL: 25 Is it your opinion, sir, that the

		Page	69
1	Boyer-Moore algorithm is a search whose execution		
2	time scales with a less-than-linear relationship to		
3	the size of the dataset to be searched?		
4	A In the worst case, no.		
5	Q Why not?		
6	A As we discussed, in the worst case, this		
7	number, i, can be as large as N minus patlen. And		
8	then the complexity is linear in N.		
9	Q When we read paragraph 72, are you		
10	conveying to the reader that the Boyer-Moore		
11	algorithm is sublinear with respect to the size of		
12	the dataset being searched?		
13	A No. All I do is quote a part of a paper		
14	that shows why that algorithm is much faster than		
15	brute force. That's all I'm doing. You're		
16	inferring things I'm not saying or writing.		
17	Q Well, when it says, "On the average, the		
18	Boyer-Moore algorithm has a sublinear behavior," are		
19	you trying to convey that that means sublinear with		
20	respect to the size of the dataset being searched?		
21	A I quoted their paper, which is this		
22	Exhibit 1017. The usual comparison is with		
23	brute-force algorithms. Okay? So if I my		
24	recollection is that this notion of sublinearity		
25	there was in comparison with a brute-force search		

		Page	70
1	algorithm. That's my recollection.		
2	Q When you quoted this language		
3	withdrawn.		
4	You could have quoted language from dozens		
5	of different papers; right?		
6	It's all possible; right?		
7	A It's possible.		
8	Q You had to select which paper to quote		
9	from; right?		
10	A Yes.		
11	Q And you had to select which sentence to		
12	quote; right?		
13	A Yes. This is simply to illustrate the		
14	point that there are much faster ways which are		
15	sublinear relative to brute-force search to do a		
16	search. This is only meant to be an example.		
17	As I said, there are many ways why Iwamura		
18	teaches that the search is sublinear. We don't even		
19	have to go into Boyer-Moore. There are many other		
20	ways in that pattern that show sublinearity.		
21	Q Well, I need to talk about the ways that		
22	you put in your Declaration.		
23	A Right.		
24	Q Now, when you were writing your		
25	Declaration, did you try to identify the clearest		

example of sublinearity in Iwamura? 1 2 Α At the time I wrote my Declaration, the Board had not come up with its claim construction. 3 After I read the claim construction by the 4 5 Board, I rethought all my assumptions, including, of 6 course, about sublinear. And I have found many 7 other reasons why Iwamura teaches a sublinear method. 8 I didn't ask you about "after." 9 0 10 Why aren't you answering my question? 11 That's the way it happened. After -- you Α 12 asked me why did I think a certain way back then and 13 why have I supplemented my views now. No, I didn't ask you about supplementing 14 Ο 15 your views. 16 Okay. Can you repeat the question. Α I'm asking you about when you wrote 17 Sure. Ο 18 this. 19 Α Yes. 20 This is the paragraph in your report where 0 you discuss whether or not Iwamura teaches 21 22 sublinearity; right? 23 Α Yes. 24 You don't have any other paragraph in your 0 report where you say, "Here's where Iwamura 25

Page 72 discloses a sublinear time search"; right? 1 I would have to double-check that. 2 Α Well, you've got a claim chart in addition 3 Q to this text; right? 4 5 Α Okay. Yes. 6 So let's go look at the claim chart. Ο 7 And if we look at --8 А It's page 29; right? If you look at the top of page 29, there's 9 Ο Element (b) from Claim 1. 10 11 Do you see that? 12 Right. Α Yes. That's the claim that has the sublinear 13 Ο portion; right? 14 15 Yes. Yes. Α 16 So if you're asking me why, well, I gave one element. You know, this chart is big enough as 17 it is. There are many claims. Again, there are 18 many other elements. And the element that was given 19 20 there is that Iwamura discloses searching using an 21 algorithm that's faster than -- much faster than 22 brute force. 23 Now, what you wrote here -- you're talking 0 24 about your claim chart on page 29; is that right? 25 А Yes.
And you're talking about the top box? 1 Q 2 Α Yes. You wrote, "Iwamura discloses searching 3 Q using the Boyer-Moore algorithm," and then you've 4 5 got a cite to Iwamura; right? 6 А Yes. And then you say "which is sublinear"; 7 Ο 8 right? 9 Α Yes. And what you meant by that was that 10 Ο Boyer-Moore is faster than brute force; is that 11 12 right? 13 Because I quoted from this Α Yes. Exhibit 1017, yes. 14 What you were trying to convey when you 15 Ο wrote that is that Boyer-Moore is faster than brute 16 17 force? 18 Α Yes. 19 Would you agree that if you were to write 0 this more clearly so that it accurately conveyed 20 21 what you meant, it would read, "Iwamura discloses 22 searching using the Boyer-Moore algorithm, which is faster than brute force"? 23 24 I don't know if I would say it that way, Α 25 You are putting words in my mouth. no.

		Page 74
1	Q What's the clearest way to say what you	
2	wanted to say when you wrote that sentence?	
3	A This is a factual statement. So	
4	Boyer-Moore is much faster than brute force. If you	
5	look at the asymptotics, the complexity of	
6	Boyer-Moore relative to brute-force search can go to	
7	zero, which indicates sublinearity.	
8	Q Well, are you saying that the Boyer-Moore	
9	algorithm is one where, as the size of the database	
10	increases, the the execution time will be	
11	increased at a less-than-linear relationship?	
12	A I did not say that, no.	
13	Q Okay. When you wrote this, were you	
14	trying to convey that Iwamura discloses searching	
15	using the Boyer-Moore algorithm, which is much	
16	faster than brute force?	
17	A Yes. This is the primary motivation of	
18	why Iwamura would use that algorithm. It's much	
19	faster than brute force.	
20	Q When you wrote this, were you trying to	
21	convey that searching using the Boyer-Moore	
22	algorithm would be sublinear with respect to the	
23	size of the dataset being searched?	
24	A No. I did not no.	
25	Q Why did you use the word "sublinear"?	

Page 75 Because I quoted from this Exhibit 1017. 1 Α 2 My question, sir, is did you quote it Ο because you wanted to indicate that Boyer-Moore --3 the Boyer-Moore algorithm was sublinear? 4 5 Okay. This reference, like many other Α 6 references, compares fast algorithms, such as 7 Boyer-Moore, with brute-force search. This 8 algorithm has a complexity that is much lower than 9 brute force. So I'm simply quoting a well-known 10 fact about Boyer-Moore. 11 If you read most papers on search, when 12 they compare it with the brute force, they say 13 Boyer-Moore and their variants are sublinear relative to brute-force search. That's all I'm 14 doing. I'm quoting a reference that says that. 15 16 So you were using this to refer to -- that Ο 17 Boyer-Moore was sublinear as compared to brute 18 force; is that right? 19 Under the proper assumptions, yes. А 20 Did -- when you wrote this, do you think Ο 21 that it would be possible -- did you consider that 22 some -- withdrawn. 23 When you wrote this sentence here on 24 page 29, did you think that someone at the Board 25 looking at this might think that you meant that a --

1 the Boyer-Moore algorithm was sublinear as used in 2 the patent claim? I didn't think of it that way, no. 3 A Well, you could have chosen a lot of 4 Ο 5 different words there. Instead of saying it's 6 sublinear, you could have said that it's faster than brute force. 7 8 You could have written that instead; right? 9 10 I quess I could have. This is a document Α 11 I wrote, you know, many months ago. It's one of 12 four documents. It has 90 pages. If you ask me why 13 did I write these words or why did I quote that paper and why not another one, it's hard to say. 14 15 0 Well, take a look at claim language on the left side. 16 17 Yes. Α 18 You wrote that sentence right next to the Ο 19 claim language that says, "Perform a sublinear time search of extracted features" --20 21 Α Right. 22 0 -- do you see that? 23 Α Yes. 24 Did you write the sentence, "Iwamura Ο discloses searching using the Boyer-Moore algorithm, 25

1 which is sublinear," to indicate that the

2 Boyer-Moore algorithm would be a sublinear time 3 search?

A I wrote that -- again, I'm trying to 5 remember how I thought several months ago, when I 6 wrote that paragraph.

7 I wrote -- again, in view -- there was no
8 claim construction at the time; so I was reading
9 about the ways in which the search can be improved
10 over brute-force search. And I just referred to an
11 element that's disclosed in Iwamura. As I said,
12 there are many other reasons about why Iwamura
13 discloses his linear search technique.

14 When you wrote your Declaration, you had 15 in mind that sublinear meant having execution time 16 that increased at a less-than-linear relationship 17 compared to the size of the dataset being searched; 18 right? 19 That's in the context of database search, A 20 yes. 21 And then you wrote this claim chart in Q 22 order to indicate where in Iwamura it disclosed each 23 part of the claim; right? 24 A That's correct, yes. 25 And next to the phrase "a sublinear time 0



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1	Boyer-Moore, as this alone, is going to give us a
2	sublinear time search in a database search problem.
3	I'm not claiming that. And I did not claim it in
4	this document.
5	Q Well, do you see how someone might read it
6	as that claim?
7	A I different people can read things
8	differently. All I know is what I just told you.
9	Q Would it be reasonable for the Board to
10	have read this as you opining, you asserting, that
11	Iwamura discloses a sublinear time search because it
12	discloses searching using the Boyer-Moore algorithm,
13	which is sublinear?
14	A Again, I don't know how different people
15	can read it. If there's any ambiguity, I hope I
16	just cleared it up. I'm not claiming that
17	Boyer-Moore alone is going to give us a sublinear
18	time search for the database search problem.
19	Q To be candid with the Board, wouldn't it
20	have been better to say, "Board, the Boyer-Moore
21	algorithm is linear, not sublinear"?
22	A Listen, there are many words that I I'm
23	sure I could have chosen better words. So I agree
24	with you, there is probably better ways to write
25	this. I don't dispute that.









1 correct?

2	A As far as I remember, yes. In that
3	Declaration at that time, yes.
4	Q The only testimony you presented to the
5	Board to to establish that Iwamura discloses
6	searching using a sublinear time search is that
7	Iwamura discloses searching using the Boyer-Moore
8	algorithm; correct?
9	A That's before they made the claim
10	construction about sublinear. Once they made the
11	claim construction, I found additional reasons why
12	Iwamura clearly discloses his sublinear search.
13	Q Again
14	A So at that time, this is the reason that I
15	incorporated it, and there are additional reasons.
16	Q How does the Board's construction differ
17	from the construction that you used when you
18	prepared your report?
19	A Well, I need to look at the precise
20	language they used for claim construction.
21	Can can I see this?
22	Q That they used or you used?
23	A That they used.
24	MR. DOVEL: I've marked as Exhibit 6-237 the
25	Board's decision with respect to the '237 patent.

Page 84 (Exhibit 6-237 was marked for 1 2 identification by the court reporter and is 3 attached hereto.) 4 MR. DOVEL: I'm going to place a copy of that 5 in front of the witness. 6 THE WITNESS: Yes. I want to compare that 7 with my own claim --8 BY MR. DOVEL: 9 Ο I'd like you to look at page 7, the Board's decision. And you will see that the Board 10 quotes both your definition and the patent owner's 11 12 on that page, and then offers its own. 13 Do you see that? Let me just read the -- the 14 Α Yeah. 15 construction. 16 Okay. So their construction is, "A sublinear search is a search whose execution time 17 scales with a less-than-linear relationship to the 18 19 size of the dataset to be searched," which is not 20 identical to what I had. Let me try to find my own construction at the time. 21 22 Ο When you say it's "not identical," it's not identical word-for-word, but it means the exact 23 24 same thing; right? 25 Well, let me just review the way I wrote Α

Page 85 Okay? Because if you are asking me about 1 it. 2 precise words, I want to make sure I'm using the 3 right words. 4 Okay. So it was 53 and 54 in my 5 Declaration. 6 Okay. So I wrote, "A sublinear search" --7 in paragraph 53 -- "means a search whose execution 8 time has a sublinear relationship to database size." 9 So the two definitions are consistent, but they are 10 not identical. 11 So once I read the constructions of the 12 Board -- not just on sublinearity, but on 13 everything -- I reevaluated all my -- my opinions. My opinions have not changed. I -- I supplement --14 15 I can supplement them, but my opinions about the anticipation and so on has not changed the least 16 17 bit. 18 Now, would you agree, sir, that the Ο 19 construction that the Board applied is consistent 20 with the construction that you applied with respect to sublinear? 21 22 Ά Yes. 23 Was there anything that's in the Board's Ο construction that's materially different than the 24 25 construction that you applied?

It is not the same language. 1 Α It is 2 slightly different, but it is consistent. Is there anything about the different 3 Ο language that results in a different meaning for the 4 5 Board's construction than yours? 6 Α It's the same -- you could say it's the 7 same meaning. They are essentially equivalent. 8 0 Would you agree, sir, that the Board's construction of sublinear didn't do anything to 9 10 change your opinions? 11 А It made me reevaluate my assumptions. 12 There's a way I think as a researcher. 13 When I read a paper or resource, it usually makes me rethink all my assumptions. And it could be I have 14 read something that even decodes what I thought 15 about before. 16 17 When I read the Board's decision, it made 18 me think, you know, in -- in, sometimes, ways that 19 can supplement what I wrote. And, again, I found 20 other reasons why Iwamura discloses a sublinear 21 search. 22 MR. DOVEL: I'm going to place in front of the 23 witness Exhibit 1010, which is the Ghias patent. 24 11 25 11

		Page	87
1	(Exhibit 1010 was marked for identification		
2	by the court reporter and is attached		
3	hereto.)		
4	BY MR. DOVEL:		
5	Q I'd like you to turn to Column 6.		
6	A Yes.		
7	Q Now, on Column 6, starting at line 23,		
8	Ghias has a discussion of several algorithms that		
9	are developed to address the problem of approximate		
10	string matching.		
11	Do you see that?		
12	A Yes.		
13	Q And then Ghias discusses the running times		
14	for those algorithms.		
15	Do you see that?		
16	A Yes.		
17	Q "Running times" here was the same as		
18	execution time?		
19	A If you have a single processor, yes.		
20	Q What Ghias discloses here are algorithms		
21	whose performance is linear with respect to the size		
22	of the dataset that's being searched; is that		
23	correct?		
24	A Well, let me review what the symbols are.		
25	N and M. So M here is number of pitch differences		

in the query, and N is the size of the string, which 1 2 is a song here. 3 I need an answer to my question. Q 4 Α I'm sorry. What was your question? 5 Sir, is it the case that Ghias, in Yeah. 0 6 Column 6, lines 23 to 35, identifies algorithms 7 whose search time scales at a linear relationship to 8 the size of the dataset being searched? 9 Α It's the string. Okay? That's why I clarified. Okay? The -- what you call the "dataset 10 11 being searched" here is the string. So N is the 12 size of the string. Okay. You've told me that N is the size 13 \bigcirc 14 of the string; right? 15 A Yes. Yes. 16 Does this indicate to you, if you read Ο 17 this, that these algorithms are linear with respect 18 to the size of the dataset being searched? 19 They're at most linear. It says or the --А of -- "On the order of." It means -- this notation, 20 21 again, means at most linear. 22 Does the information that's presented here 23 suggest to you that these -- that these algorithms 24 are sublinear with respect to the size of the 25 dataset being searched?

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		Page 89
1	A It does not say that. First, there's no	
2	database. Okay? Again, this refers to a single	
3	song.	
4	Q Well, when it says "string," string would	
5	be a dataset; right?	
6	A If you view a song as a dataset, fine.	
7	Q Do you view it that way?	
8	A Well, I'm just reading from what Ghias	
9	wrote. And because they're, of course, in that	
10	problem, there's a database that has many songs.	
11	So just to make it clear, N is not the	
12	size of the database; N is the size of a single	
13	song.	
14	Q Reading this, do you interpret this to	
15	suggest that these algorithms are sublinear with	
16	respect to the size of the dataset being searched?	
17	A No. This, again, reads "of the order of."	
18	So it means at most linear.	
19	Q And what does it tell us about the	
20	performance of these algorithms withdrawn.	
21	What does this paragraph tell you about	
22	the execution time of these searches with respect to	
23	the size of the dataset being searched?	
24	A It only speaks about the size of the of	
25	the song. And what is written there is a comparison	
1		

between these fast-matching algorithm and -- and 1 brute force, which is exactly like in Boyer-Moore 2 that we just discussed. It's the exact same 3 4 concept. 5 Does this tell us -- withdrawn. \bigcirc 6 When you read this, did this indicate to 7 you that these algorithms were ones that would be 8 used to perform a sublinear search with respect to 9 the size of the dataset being searched? It's the same issue as with Boyer-Moore 10 Α 11 that we just discussed. So relative to brute force, which is complexity order MN, these fast algorithms, 12 13 okay, such as Baeza-Yates and Gonnet, have a search complexity that vanishes as M times N goes to 14 15 infinity. 16 My question, sir, is did you read this to 17 indicate or suggest that these algorithms would --18 could be used to perform a sublinear time search 19 with respect to the size of the dataset being 20 searched? 21 A No. 22 Ο At any point, did you ever read this and say, "Aha, these algorithms here teach a sublinear 23 24 time search as it's used in the '237 patent"? 25 "These algorithms" -- I'm just reading Α

1	here "teach that they are fast search
2	algorithms," okay, "for this problem of matching a
3	pattern into a song that are much faster than brute
4	force." Okay?
5	Q Did you, at any point, ever read this
6	portion of Ghias and say to yourself, "This teaches
7	a sublinear time search as it's used in the '237
8	patent"?
9	A It teaches to of a search that is much
10	faster than brute force. Again, Ghias, just like
11	Iwamura, disclose sublinear search in many ways.
12	So this paragraph we're discussing alone
13	does not discuss does not disclose sublinear
14	search, possibly. Sublinear search is disclosed
15	many other ways through through that patent.
16	Q Well, I'm talking about this passage here.
17	A Right.
18	Q Did you ever read this and say to
19	yourself, "What it says here about these algorithms,
20	in this description of these algorithms, tells me
21	that we have a sublinear time search"?
22	A No. I don't represent that, no.
23	Q Did you look up these papers here to see
24	what these algorithms were?
25	A Yes, I looked them up.

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1	Q Did the Ricardo Baeza-Yates paper, the		
2	first one or the second one, did they disclose a		
3	sublinear time search with respect to the size of		
4	the dataset being searched?		
5	A Again, what you call "the dataset" is a		
6	string. Okay? And so these algorithms, if I		
7	remember well, disclose a sublinear complexity		
8	relative to brute force.		
9	Q That wasn't my question.		
10	A Okay. Can you rephrase it		
11	Q Sure.		
12	A Can you restate your question.		
13	Q Did you look up these algorithms that are		
14	described here in Columns 6, lines 23 to 35, to		
15	determine whether they disclosed algorithms that		
16	would do a search that was sublinear with respect to		
17	the size of the dataset being searched?		
18	A Again, the dataset, in this context of		
19	those papers, is a single string. It's not a		
20	database, okay, it's a single string. These papers		
21	quote formulas that indicate sublinearity relative		
22	to brute-force search. That's all they do.		
23	I'm not, again, representing that using		
24	those algorithms alone are going to give us a		
25	sublinear complexity for searching the data the		

entire database of songs. I don't represent that, 1 2 to make it clear. 3 MR. DOVEL: Yeah. Let's take a break, and 4 we'll change our tape. 5 MR. ELACOUA: Sure. 6 THE VIDEOGRAPHER: This marks the end of 7 Videotape Number 1 in the deposition of Pierre Moulin. We're off the record at 11:06 AM. 8 9 (Off the record.) THE VIDEOGRAPHER: We are back on the record 10 11 at 11:15 AM. This marks the beginning of Videotape 12 Number 2 in the deposition of Pierre Moulin. BY MR. DOVEL: 13 I want you to look at the Ghias reference 14 0 15 again. That's Exhibit 1010. In Column 6, starting at lines -- line 36 16 through 59, Ghias describes using an algorithm and 17 18 what the performance of the algorithm would be. 19 Do you see that? 20 Α Let me read the whole section. So you say 36 to 59? 21 22 Ο Yes. 23 Okay. Α 24 Does this portion of Ghias, Column 6, 0 25 lines 36 through 59, does that describe a search

1	algorithm whose execution time is sublinear with
2	respect to the size of the dataset being searched?
3	A No, it does not, again, because we see
4	it's with respect to the size of the dataset being
5	searched, which is a song, a single song here.
6	Q And why doesn't that disclose a sublinear
7	time search?
8	A Well, for many reasons. So first, it's
9	the order of notation, which always means at most,
10	something.
11	Second, you know, there's always the issue
12	of worst-case scenario and average performance; so
13	these are quite different. So it simply does not
14	disclose that. And also, the reference, again, is
15	brute force. Okay? So it compares with this O(mn)
16	for brute-force search.
17	Q Is it the case that what is disclosed here
18	is a search whose execution time would scale at less
19	than a linear relationship to the size of the
20	dataset being searched?
21	A Possibly. It depends on parameters, such
22	as K. They even give you an example there.
23	"When K is equal to M" this is line 43
24	through 46 or 45 "then the search is immediate."
25	Okay. So so it's obviously sublinear in that

1 case. When you say, "When K equals M," what do 2 Ο you mean by, "When K equals M"? 3 So this is line 43, starting with "K 4 Α 5 equals M." 6 And what does "K equals M" indicate? What 0 7 does that mean? 8 Α Well, K is number of mismatches, and M is 9 the length of the query. So that's when you've got a particular 10 0 problem where the number of mismatches is the same 11 12 as the number of the query? 13 Α That's right. And then the search stops after only one step. 14 If we have a search where we don't have a 15 Ο known or fixed number of mismatches that -- set to 16 the length of the query, does this tell us anything 17 18 about whether we've got a sublinear search? 19 The algorithm must tell you -- you Α No. 20 must input K into the algorithm. So if you say, "I don't know K," you cannot run the algorithm. 21 22 Ο Is K the number of allowed mismatches? 23 Α K -- let's see the way they define it. 24 So this is on line 37. "The algorithm addresses the problem of string matching with K 25

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1	mismatches." So it's exactly K.		
2	Q All right. Is are you saying that if		
3	somebody knew how many mismatches you had, then you		
4	could input a specific K?		
5	A That's what K is. So if you know there		
6	are three mismatches, then K is equal to three.		
7	Q What's a mismatch?		
8	A Mismatch. So if I have a single string of		
9	English text, okay, so if the two letters I'm		
10	comparing are the same, there's no mismatch, and in		
11	any other case, there is a mismatch.		
12	Q Are you saying that that you're going		
13	to be allowing for up to three mismatches?		
14	A For exactly three mismatches. That's what		
15	this says.		
16	Q Okay.		
17	A Lines 36, 37.		
18	Q It says, "If there are no mismatches, we		
19	have a simple string matching problem." And by		
20	that, you mean if there's no mismatches, that would		
21	mean that we are going to find our string exactly		
22	matched or our query exactly matched someplace in		
23	the string; is that right?		
24	A We'll try to find it. It may not be		
25	there.		